

# ECB Workshop on Forecasting Techniques

## “The Anatomy of Out-of-Sample Forecasting Accuracy”

by Borup, Coulombe, Rapach, Schütte and Schwenk-Nebbe

Discussion by Michel van der Wel

Erasmus U Rotterdam

June 13, 2023



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  - Two metrics for importance of individual predictors for predicted target values
  - New metric (PBSV) for contribution of individual predictors for loss in sequence of fitted models



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- Paper develops Shapley-based metrics for interpreting models
  - Two metrics for importance of individual predictors for predicted target values
  - New metric (PBSV) for contribution of individual predictors for loss in sequence of fitted models
- Empirical study of forecasting US inflation provides sensible leading predictors (oil, components of CPI) and discrepancies between in-sample and out-of-sample importance



# Shapley values

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$$\phi_p = \sum_{Q \subseteq S \setminus \{p\}} \frac{|Q|!(P-|Q|-1)!}{P!} (E[f|Q \cup \{p\}] - E[f|Q])$$



# Shapley values

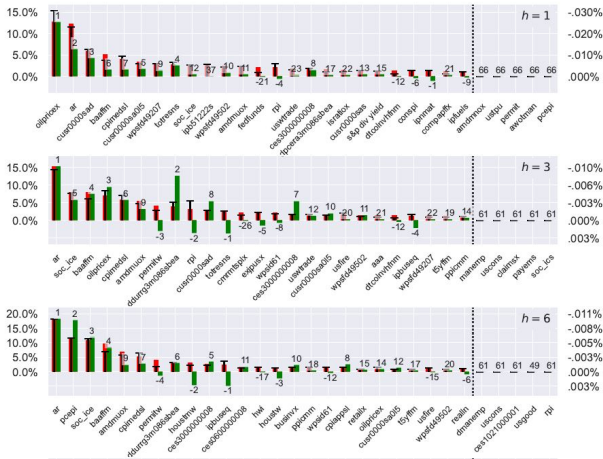
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- Paper cleverly adjusts setting for
  - Dealing with large number of predictors (use sampling)
  - Expanding samples (not one value; take average)
  - Retraining of the samples  $\rightarrow$  (i/o)Shapley-VI $_p$
  - Loss-function effects rather than predicted values  $\rightarrow$  PBSV $_p$



# 1. Empirical findings (Figure 1)



- Stability of findings (pcepi least to 2nd most important  $h = 1$  to  $h = 6$ )?
- Why not more correlated results (similar series in FRED-MD)?

## 2. Empirical application

- Curious to robustness regarding
  - Forecasting  $y_{t+h}$  rather than  $\frac{1}{h} \sum_{k=1}^h y_{t+k}$
  - Including predictors and moving average of predictors
  - Selection of  $L$  (AR-lag) and  $q$  (MA-order)



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- Main benchmark is AR( $k$ ) model. Consider smaller/more targeted model with explanatory variables, survey data, etc? Particularly given somewhat modest (short-horizon) improvement of ML approaches (7% for  $h = 1$ ; 19% for  $h = 12$ )



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- For PCA, possible to compare with significance?

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Overes and Van der Wel (Computational Economics; 2023) also use Shapley values (for driving factors of sovereign credit ratings). From referee process:

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- Can you take the panel nature into account? [You do!]
- Compare to `scikit-learn` package (which also provides feature importance estimates)
- Closer comparison of findings with existing literature and evaluation also of signs

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In conclusion:

- Opens the black box with clever adaptations to time series setting
- Great work!

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