

Financial indicators and density forecasts for US output and inflation

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The presentation does not reflect the official view of Banca d'Italia.

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Questions

- Are financial indicators useful in forecasting output and inflation?
- Does the answer depend on what kind of **events** the forecaster is interested in predicting? (central case/bad scenarios)
- Does the answer depend on what kind of **models** the forecaster relies on? (linear/nonlinear)
- Was the Great Recession predictable on the basis of real-time financial information?

Answers/conjectures

- 1 Yes (with qualifications)
- 2 Yes: financial info might be particularly useful in predicting "tail outcomes" and recessions.
- 3 Yes: nonlinear models account for the fact that the role of financial markets in generating/propagating shocks may change over time.
- 4 No idea

The paper in a nutshell (1)

Data and models

We cast the analysis as a density prediction problem:

$$pdf^m(y_{t+k} | I_t) = m(y_t, f_t, X_t)$$

- Monthly US data, 1973-2012
- y_t : industrial production growth, CPI inflation.
- f_t : Financial Condition Index (FCI) published by St Louis Fed.
- m : linear VAR *versus* Threshold VAR (potentially capturing normal times/crises).

The paper in a nutshell (2)

Results

- 1 VAR gives better point forecasts.
- 2 TAR gives better density forecasts.
- 3 f_t improves both, but works best in density space: finance helps in predicting off-equilibrium paths.
- 4 TAR with finance-driven regimes could have anticipated (up to a point...) the Great Recession.

Broader implications:

- Non-linearities matter

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Broader implications:

- Non-linearities matter
- Predictive distributions are useful to study the finance-macro nexus
- Given (1, 2), objectives and risk preferences of the forecaster become crucial.

Literature (1)

- 1 Forecasting with financial indicators (Stock-Watson 2003, 2012; Gilchrist-Yankov-Zakrajšek 2009, 2012; Ng-Wright, 2013; ...). Emphasis on point forecasts and linear models.
- 2 Density forecasting in macro (eg. Clark, 2011). No specific analysis of the role of financial factors.
- 3 Early warnings and crisis prediction (Borio-Lowe, 2002; Barro-Ursua, 2009; Lo Duca-Peltonen, 2011). Low frequency data and arbitrary/restrictive definition of "crises".

This paper

Contributes to (2), proposes density forecasting as a generalisation of (1) and a link between (1) and (3)

- 4 GE models with financial shocks (Gertler-Kiyotaki 2010; Jermann-Quadrini 2012; Kiyotaki-Moore 2012; Liu-Wang-Zha 2013; ...). GE models with occasionally binding credit constraints (Bianchi 2012; Bianchi-Mendoza 2011; Guerrieri-Iacoviello 2013).
- 5 Evidence of nonlinear, regime-dependent, transmission of macrofinancial shocks (McCallum 1991; Balke 2004; GI 2013). Emphasis on impulse-response analysis.

Bottomline: financial shocks matter, and may have different implications in good and bad (credit-constrained) times.

This paper

Studies/exploits the nonlinearity modelled in (4) and documented in (5) from a forecasting perspective (see toy P.E. model in the paper)

- Data
- Models
- Simulating and evaluating distributions
- Results
- Conclusions

US data, March 1973 – August 2012.

y_t : Industrial Production growth

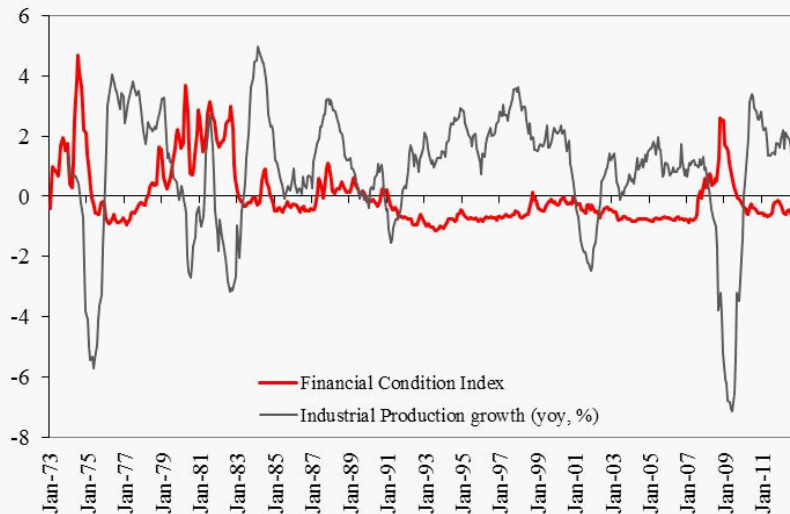
π_t : CPI inflation

r_t : Fed Funds rate

f_t : Financial Conditions Index

FCI is a dynamic factor constructed from an unbalanced panel of 100 mixed-frequency indicators of financial activity (Brave & Butters 2012; Chicago Fed). Real time, very broad coverage (debt and equity markets, financial sector leverage, ...).

Financial Condition Index



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Financial information and non-linearities on a 2x2 grid:

| | NO FINANCE | FINANCE |
|-----------|------------|---------|
| LINEAR | VAR^S | VAR |
| NONLINEAR | $(MSVAR)$ | TAR |

- VAR^S = linear VAR without f_t

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- TAR = two-state Threshold VAR with regime switches caused by f_t
- $(MSVAR = \text{Markov-switching VAR, not shown for brevity})$

$$Y_t = c + \sum_{j=1}^P B_j Y_{t-j} + \Omega^{1/2} e_t, \quad e_t \sim N(0, I) \quad (1)$$

We set $P = 13$ and study two specifications

- VAR^S : $Y_t = (y_t, \pi_t, r_t)$
- VAR : $Y_t = (y_t, \pi_t, r_t, f_t)$

Natural conjugate prior (N, IW) as in e.g. Banbura-Giannone-Reichlin (JAE, 2010). All variables treated as independent AR(1) processes:

$$\begin{aligned} Y_t &= c + \Gamma Y_{t-1} + \Sigma e_t \\ \Gamma &= \text{diag}(\gamma_1, \dots, \gamma_N) \\ \Sigma &= \text{diag}(\sigma_1, \dots, \sigma_N) \end{aligned}$$

$$Y_t = c_{S_t} + \sum_{j=1}^P B_{S_t,j} Y_{t-j} + \Omega_{S_t}^{1/2} e_t, \quad e_t \sim N(0, I) \quad (2)$$

$$S_t = \{0, 1\} \quad (3)$$

$$S_t = 1 \iff f_{t-d} \leq f^* \quad (4)$$

where $Y_t = (y_t, \pi_t, r_t, f_t)$. Note f_t impacts (y_t, π_t, r_t) through $B_{S_t,j}$ and drives the transitions across regimes.

Symmetric natural conjugate prior for the two regimes, plus agnostic prior for (f^*, d) :

$$f^* \sim N\left(\frac{\sum_t f_t}{T}, \bar{k}\right)$$

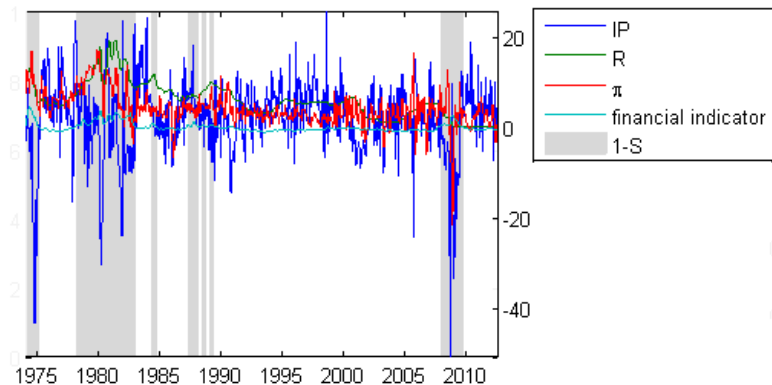
$$d \sim U\{1, \dots, 13\}$$

Note: the priors are uninformative and a-theoretical. One could use theory to impose structure on the differences between regimes.

- Bayesian approach
- VAR posterior is known analytically (Banbura et al, 2010).
- TAR and MSVAR posteriors can be simulated by Gibbs sampling (Chen & Lee, 1995; Amisano & Fagan, 2010)
- For each estimation we use 20,000 Gibbs sampling draws and discard the first 15,000

Estimation results (1)

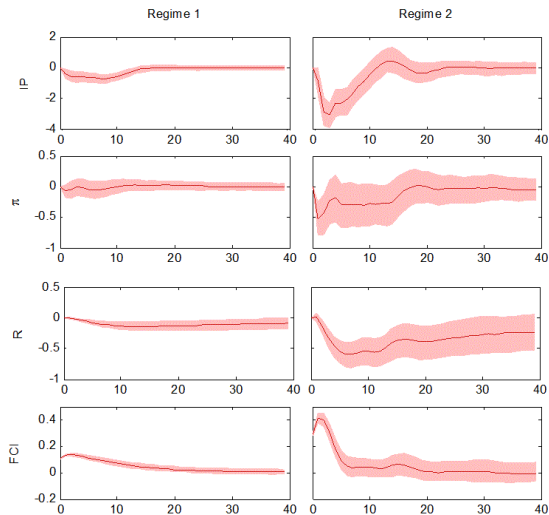
Financial regimes.



$(1 - \hat{S}_t) = 1 \Leftrightarrow f_{t-d} > f^* \Leftrightarrow$ financial distress/binding credit constraints

Estimation results

A one standard deviation financial shock (recursive identification)



- Data
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- **Simulating and evaluating distributions**
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Generating the predictive pdfs

Simulation strategy

Collect model's m parameters into Θ_t . The k -periods ahead PD is:

$$\begin{aligned} p_t^m &\equiv p^m(Y_{t+k} | Y_t) \\ &= \int p(Y_{t+k} | Y_t, \Theta_{t+k}) p(\Theta_{t+k} | Y_t, \Theta_t) p(\Theta_t | Y_t) d\Theta \end{aligned}$$

Simulating the PD:

- 1 draw Θ_t from the posterior (3rd term)
- 2 simulate forward any time-varying parameters (2nd term)
- 3 use Θ_{t+k} to simulate paths for Y_{t+k} (1st term).

Generating the predictive densities

Models and data

- $m = VAR^S, VAR, TAR$
- Recursive exercise: we start from 1973.03–1983.04 and reestimate all models adding one observation at a time.
- For each estimation sample $\{Y_{1,\dots,T}\}$ we simulate the models up to $K = 12$ months ahead.
- This gives us a set of 354 out-of-sample density forecasts $p^m(Y_{T+k} | Y_T)$ per model.

Evaluating the predictive densities

1. Calibration

Is any of the models "right"?

Probability integral transforms (**PIT**), probability coverage ratios (**PCR**)

Intuition: the data should fall evenly across model-generated percentiles.

2. Accuracy

How to compare a pair of (potentially misspecified) models?

Log-scores (**LS**), predictive Bayes factors (**BFs**)

Intuition: higher LS for models attaching higher likelihood to the events that actually occurred.

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- RMSE and LS rank the models in a very different way:

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- Most of these differences are predictable to some extent.

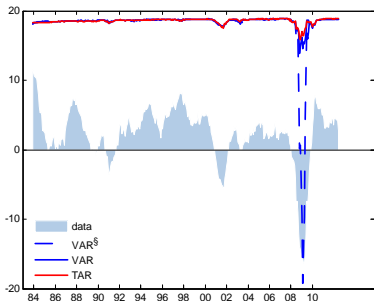
Results

RMSE/LS for output and inflation

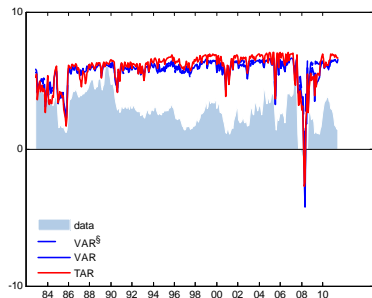
| | | RMSE | | | | LS | | | |
|------------------|----------|--------|--------|--------|--------|---------|---------|---------|---------|
| | | 1M | 3M | 6M | 12M | 1M | 3M | 6M | 12M |
| VAR ^S | <i>y</i> | 5.604 | 6.465 | 6.804 | 7.019 | -3.674 | -3.338 | -3.418 | -3.948 |
| | <i>r</i> | 0.167* | 0.357 | 0.598 | 0.985 | -0.675 | -1.380 | -1.754 | -2.118 |
| | π | 2.078 | 2.607* | 2.812* | 3.077* | -2.584 | -2.658 | -2.266 | -2.137 |
| | <i>f</i> | - | - | - | - | - | - | - | - |
| VAR | <i>y</i> | 5.446* | 6.166* | 6.558* | 6.912* | -3.553 | -3.156 | -3.032 | -2.964 |
| | <i>r</i> | 0.177 | 0.365 | 0.602 | 0.989 | -0.645 | -1.357 | -1.723 | -2.101 |
| | π | 2.067* | 2.620 | 2.839 | 3.115 | -2.583 | -2.550 | -2.339 | -2.171 |
| | <i>f</i> | 0.102* | 0.197 | 0.289 | 0.386 | 0.135 | -0.649 | -0.957 | -1.130 |
| TAR | <i>y</i> | 5.491 | 6.187 | 6.594 | 6.934 | -3.491* | -3.152* | -3.005* | -2.885* |
| | <i>r</i> | 0.167 | 0.338* | 0.555* | 0.943* | 0.022* | -0.778* | -1.364* | -1.999* |
| | π | 2.115 | 2.667 | 2.864 | 3.116 | -2.503* | -2.415* | -2.195* | -2.080* |
| | <i>f</i> | 0.104 | 0.190* | 0.271* | 0.367* | 0.496* | -0.122* | -0.431* | -0.717* |

* denotes best model for each criterion/variable/horizon

Industrial production growth

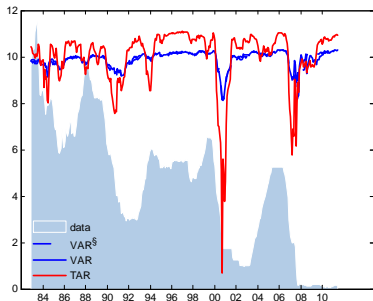


CPI inflation

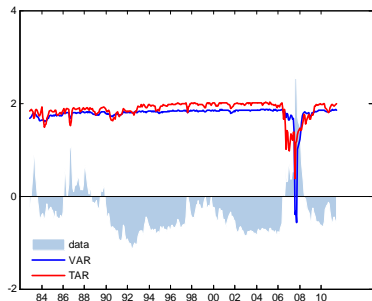


Log-Scores (2)

Policy rate

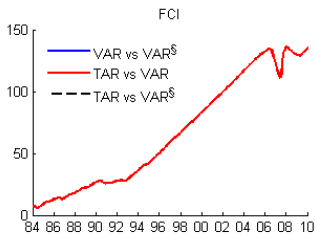
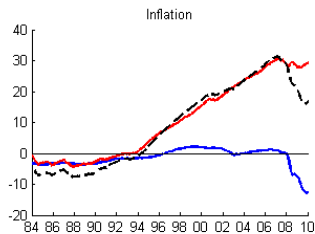
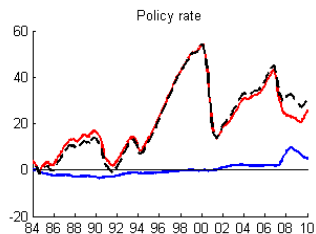
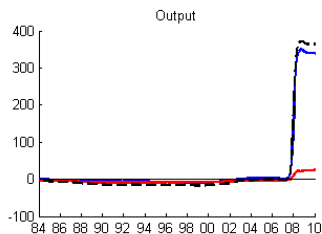


Financial Condition Index



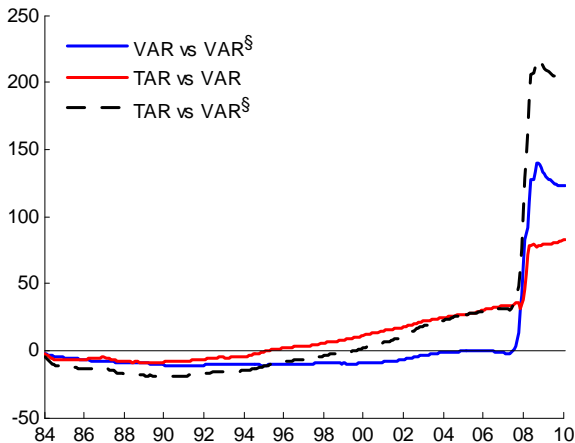
Log-Bayes Factors (1)

Marginal distributions



Log-Bayes Factors (2)

Joint distribution of IP and CPI



Giacomini-White decision criteria

Is the discrepancy between models itself predictable?

Following Giacomini-White (E 2006), we study the persistence of the *difference in performance* between pairs of models:

$$\begin{aligned}\Delta Loss_{t+\tau} &= \alpha + \delta \Delta Loss_t + \varepsilon_t \\ \text{where } \Delta Loss &\equiv Loss^{VAR} - Loss^{TAR} \\ \text{and } Loss &\equiv RMSE, -LS\end{aligned}$$

Model selection criterion:

$$Use\ TAR \iff E_t \Delta Loss_{t+\tau} > 0 \iff (\hat{\alpha} + \hat{\delta} \Delta Loss_t) > 0$$

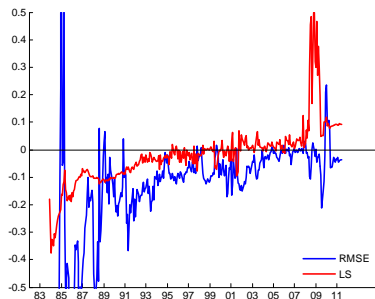
Giacomini-White decision criteria

VAR versus TAR

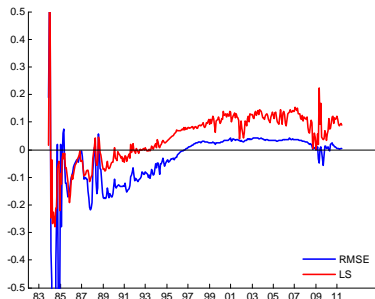
Blue (red) line = $E_t \Delta Loss_{t+12}$ for $Loss = RMSE$ ($-LS$).

Positives implies that *TAR* dominates *VAR*.

Industrial production

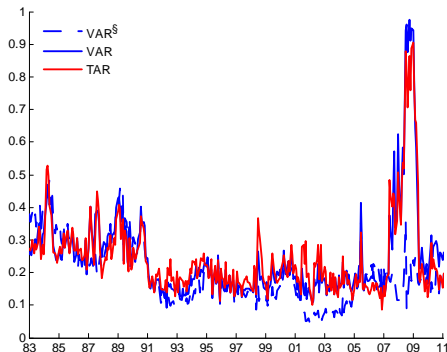


CPI inflation



Predictive densities and early warnings

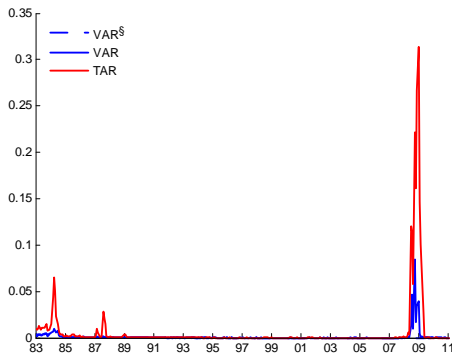
Ex-ante recession probability: $prob_t \left(\sum_{h=1}^{12} y_{t+h} < 0 \right)$



VAR/TAR virtually identical: all that matters is the presence of FCI

Predictive densities and early warnings

Ex-ante "great recession" probability: $prob_t \left(\sum_{h=1}^{12} y_{t+h} < -20\% \right)$



... But TAR anticipates a more severe downturn.

- Data: "excess bond premium" (Gilchrist and Zakrajšek, 2012) instead of Financial Condition Index.
→ Similar qualitative results.
- Models: rolling VAR, Markov-switching VAR with transition probabilities that depend on FCI.
→ Both dominated by TAR. TAR appears to capture the "right" kind of time variation in parameters.

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- 3 **Models:** VAR is better (worse) than TAR for point (density) forecasting. With imperfect models, the risk preferences of the forecaster become crucial.
- 4 **Great Recession:** essentially unpredictable – but less so for a TAR with finance-driven regimes.

- Work out distributional implications of credit constraints in a (more) general equilibrium model.
- Think formally about risk preferences and model selection.
- Refine priors on good/bad regimes
- More robustness (sample, prior hyperparameters, ...)

Thanks!

Reserve slides

Endowment economy with random income and consumption/saving decision subject to borrowing constraint:

$$\max_{(c_t, a_t)_{t=0}^{\infty}} \sum_{t=0}^{\infty} \beta^t \left(\mathcal{U}(c_t) + \mathcal{P}(a_t + \theta_t y) \right) \quad (5)$$

$$c_t + \frac{a_t}{1+r} = a_{t-1} + y_t \quad (6)$$

$$y_t = e^{z_t}, \quad z_t \sim N(0, \sigma_z) \quad (7)$$

$$\theta_t = \theta(1 - \rho_\theta) + \rho_\theta \theta_{t-1} + \epsilon_t, \quad \epsilon_t \sim N(0, \sigma_\epsilon) \quad (8)$$

- **Penalty function:** $\mathcal{P}(a_t + \theta_t y) = \phi \log(a_t + \theta_t y)$.
Borrowing ($a_t < 0$) causes disutility, with $\mathcal{P} \rightarrow -\infty$ as $a_t \rightarrow -\theta_t y$.
A trick to approximate an occasionally binding constraint:

$$\mathcal{P}(a_t + \theta_t y) \simeq a_t \geq -\theta_t y$$

- **Financial shock** ε_t : shifts the borrowing limit for a given income level. A proxy for collateral value or strength of lender's balance sheet.

Obviously a toy model, with exogenous income and interest rate, but useful to think about (linear/nonlinear) and (central/density) forecasting issue.

| | | | | | | |
|---------|------|----------|------------|----------------------|---------------|--------|
| β | r | θ | σ_z | σ_ε | ρ_θ | ϕ |
| 0.90 | 0.03 | 1 | 0.1 | 0.01 | 0.5 | 0.05 |

Made up. Low β guarantees that agents borrow in equilibrium:
 $-\theta y < a < 0$

Policy functions at II order

| | \hat{a}_{t-1} | $\hat{\theta}_{t-1}$ | z_t | ε_t | $\hat{a}_{t-1}\hat{\theta}_{t-1}$ | $\hat{a}_{t-1}z_t$ | $\hat{a}_{t-1}\varepsilon_t$ | $\hat{\theta}_{t-1}z_t$ | $\hat{\theta}_{t-1}\varepsilon_t$ |
|-------------|-----------------|----------------------|-------|-----------------|-----------------------------------|--------------------|------------------------------|-------------------------|-----------------------------------|
| \hat{c}_t | 0.264 | 0.058 | 0.263 | 0.116 | -0.068 | -0.127 | -0.135 | -0.067 | -0.085 |
| \hat{a}_t | 0.758 | -0.060 | 0.754 | -0.119 | 0.069 | 0.130 | 0.139 | 0.070 | 0.088 |

Selected terms. All in deviations from steady-state values.

- A negative financial shock $\varepsilon_t < 0$ depresses c and increases a , i.e. it leads to a cut in debt relative to equilibrium

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- Its impact is stronger when debt is already high ($\hat{a}_{t-1} < 0$) and/or borrowing conditions are tight ($\hat{\theta}_{t-1} < 0$)

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- Any prediction from a linear model ignores $a\theta$, az , $a\varepsilon$, θz , $\theta\varepsilon$

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- CFs ($E_t c_{t+1}$) from a nonlinear model leave out $a\varepsilon$, θz , $\theta\varepsilon$
- PDs ($p_t(c_{t+1})$) from a nonlinear model capture all terms.

For instance, the model should predict an increase in the *volatility* of c_t when θ_{t-1} or a_{t-1} are low (tight markets/high debt).

$$Y_t = c_{S_t} + \sum_{j=1}^P B_{j,S_t} Y_{t-j} + \Omega_{S_t}^{1/2} e_t, \quad e_t \sim N(0, I) \quad (9)$$

$$S_t = \{0, 1\} \quad (10)$$

$$S_t = 1 \iff x_t^* \geq 0 \quad (11)$$

$$x_t^* = \lambda_0 + \gamma_1 f_{t-1} + \lambda_1 S_{t-1} + v_t, v_t \sim N(0, 1) \quad (12)$$

where $Y_t = (y_t, \pi_t, r_t)$ and x_t^* is an unobserved state.

Symmetric n.c. prior for the two regimes and agnostic prior for (λ_i, γ) :

$$[\lambda_0 \quad \lambda_1 \quad \gamma_1]' \sim N\left([\ -2 \quad 4 \quad 0 \]', \bar{k}I\right)$$

The MS-VAR incorporates a more flexible/possibly weaker role for finance:

- f_t does *not* have a direct impact on (y_t, π_t) through $B_{S_t,j}$
- f_t *may/may not* influence the transitions between regimes:

$\gamma_1 < 0 \Rightarrow$ high f_t increases the prob of entering/being stuck in S_0

$\gamma_1 = 0 \Rightarrow$ fixed, exogenous transition probabilities

Different story:

here financial distress does not cause recessions, but can bring about a state with e.g. lower average output growth and/or different transmission channels for non-financial (monetary, AS, AD) shocks.

$$Y_t = c_{S_t} + \sum_{j=1}^P B_{j,S_t} Y_{t-j} + \Omega_{S,t}^{1/2} e_t \quad (13)$$

$$\begin{bmatrix} \Pr(0|0) & \Pr(0|1) \\ \Pr(1|0) & \Pr(1|1) \end{bmatrix} = \begin{bmatrix} P(f_{t-1}) & 1 - Q(f_{t-1}) \\ 1 - P(f_{t-1}) & Q(f_{t-1}) \end{bmatrix} \quad (14)$$

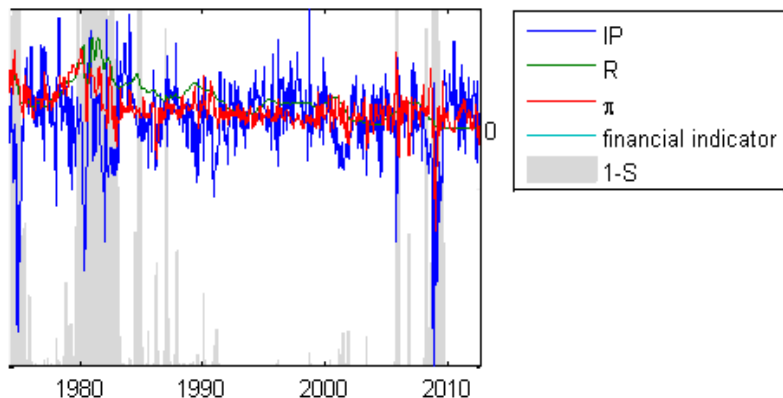
where $e_t \sim N(0, I)$, $Y_t = (y_t, \pi_t, r_t)$, and (P, Q) are Probit models:

$$P(f_{t-1}) = 1 - \Phi(\lambda_0 + \gamma_1 f_{t-1}) \quad (15)$$

$$Q(f_{t-1}) = \Phi(\lambda_0 + \lambda_1 + \gamma_1 f_{t-1}) \quad (16)$$

Estimation results, FCI specification

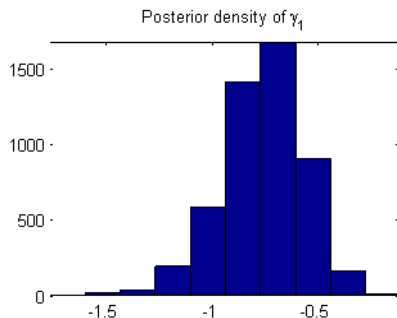
MSVAR regimes



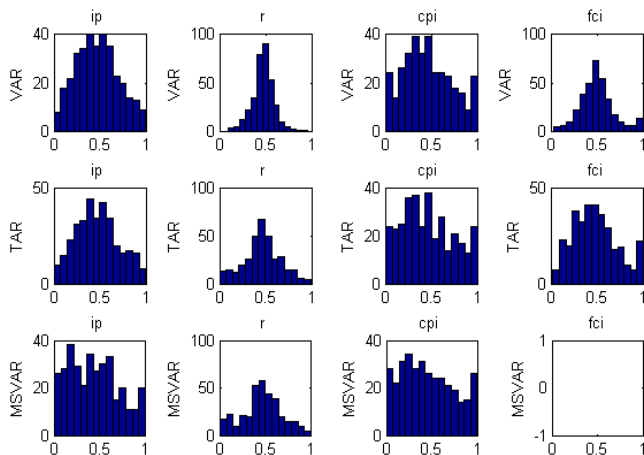
Grey area = median estimate of $\Pr(\hat{S}_t = 0)$ based on full-sample information. Continuous values in $[0, 1]$

Estimation results, FCI specification

MSVAR posterior



- $\gamma_1 < 0$: financial instability increases the likelihood of entering the bad state
- The BS indicator delivers $\gamma_1 \simeq 0$, and EBP a counterintuitive $\gamma_1 > 0$.



Amisano-Giacomini weighted LS test

| | Left tail | | | | Both tails | | | |
|----------------------|-----------|--------|---------|--------|------------|--------|---------|--------|
| | y | r | π | f | y | r | π | f |
| Weighted log-scores: | | | | | | | | |
| VAR ^S | -1.881 | -0.513 | -1.846 | - | -0.924 | -0.220 | -0.914 | - |
| VAR | -1.761 | -0.491 | -1.848 | 0.249 | -0.816 | -0.211 | -0.927 | -0.075 |
| TAR | -1.698* | 0.032 | -1.779 | 0.479* | -0.753* | 0.029 | -0.866* | 0.149* |
| MSVAR | -2.006 | 0.066* | -1.732* | - | -1.129 | 0.055* | -0.887 | - |

P-values:

| | | | | | | | | |
|------------------------|-------|-------|-------|-------|-------|-------|-------|-------|
| VAR ^S , VAR | 0.050 | 0.000 | 0.230 | - | 0.139 | 0.021 | 0.181 | - |
| TAR, VAR | 0.370 | 0.000 | 0.674 | 0.000 | 0.401 | 0.000 | 0.801 | 0.000 |
| MSVAR, VAR | 0.517 | 0.000 | 0.425 | - | 0.025 | 0.000 | 0.334 | - |
| MSVAR, TAR | 0.101 | 0.228 | 0.098 | - | 0.535 | 0.026 | 0.333 | - |

(*) denotes the best model for each variable and weighting function